



**DR-003-1016003**

Seat No. \_\_\_\_\_

**B. Sc. (Sem-VI) (W.E.F. 2016) Examination**

**April - 2022**

**Mathematics : Paper-10 (A)**

*(Optimization & Numerical Analysis-II)*

**Faculty Code : 003**

**Subject Code : 1016003**

Time :  $2\frac{1}{2}$  Hours]

[Total Marks : 70

**Instruction :** Answer any Five questions.

- 1 (A) Answer the following questions : 4
- (1) What do you mean by Artificial variable ?
  - (2) What do mean by Standard form LPP ?
  - (3) Name three different methods to solve LPP.
  - (4) In the two-phase method, \_\_\_\_\_ variable is never considered for re-entry in to the basis.
- (B) Answer any one : 2
- (1) Define : (1) Unbounded Solution  
(2) Optimum basis feasible solution.
  - (2) Define : (1) Slack variable  
(2) Surplus Variable
- (C) Answer any one : 3
- (1) Explain Primal-dual relationship.
  - (2) Explain the graphical method for optimization.
- (D) Answer any one : 5
- (1) Using Graphical method Maximize  
 $Z = 11x_1 + 9x_2$  subject to  
 $3x_1 + 2x_2 \leq 8, 2x_1 + 3x_2 \leq 7$  and  $x_1 \geq 0, x_2 \geq 0$

- (2) The manager of an oil refinery must decide on the optimum mix of two possible blending processes of which the inputs and outputs per production run are as following :

–	<i>input(units)</i>	–	<i>output(units)</i>	–
<i>process</i>	<i>Crude A</i>	<i>Crude B</i>	<i>Gasoline X</i>	<i>Gasoline Y</i>
1	5	3	5	8
2	4	5	4	4

The maximum amount available of crudes A and B is 200 units and 150 units respectively. Market requirements show that at least 100 unit of gasoline X and 80 units of gasoline Y. must be produced. The profits per production run from process 1 and process 2 are Rs. 300 and Rs.400 respectively. Solve the LP problem by graphical method.

- 2 (A) Answer the following question : 4

- (1) What is called feasible solution in Transportation Problem?
- (2) Riddhi found a transportation problem having three rows and five columns. Jigna asked her how many positive allocations be made for Basic Feasible Solution ? Anita spoke “Five” in between their talk. Riddhi replied “Nine.” Jigna said “Fifteen” What is the correct answer ?
- (3) Forum asks a question to Nisha, “What is called Optimal Solution in Transportation Problem ? What is the correct answer ?
- (4) “What is called degenerate B.F.S ?”, Jayesh asked Chirag. What was the correct answer given by him ?

- (B) Answer any one : 2

- (1) State mathematical form of transportation problem.
- (2) Find the initial solution of the following transportation problem by NWCM.

	<i>W1</i>	<i>W2</i>	<i>W3</i>	<i>Supply</i>
<i>F1</i>	2	7	4	5
<i>F2</i>	3	3	1	8
<i>F3</i>	5	4	7	7
<i>F4</i>	1	6	2	14
<i>Demand</i>	7	9	18	34

- (C) Answer any one : 3

- (1) Explain NWCM.
- (2) Explain LCM.

(D) Answer any one : 5

- (1) Find the optimum solution of the following using MODI method.

	<i>W1</i>	<i>W2</i>	<i>W3</i>	<i>Supply</i>
<i>F1</i>	2	7	4	5
<i>F2</i>	3	3	1	8
<i>F3</i>	5	4	7	7
<i>F4</i>	1	6	2	14
<i>Demand</i>	7	9	18	34

- (2) Explain Hungarian method.

3 (A) Answer the following questions : 4

- (1) To interpolate near the middle of difference table Which formula will be useful ?
- (2) Write Gauss forward interpolation formula.
- (3) Write the range of P for which the Gauss forward interpolation formula is useful ?
- (4) In which condition Laplace -Everett's formula can give accurate result ?

(B) Answer any one : 2

- (1) If  $y_2 = 10, y_1 = 8, y_0 = 5, y_{-1} = 10$  then find  $y_{\frac{1}{2}}$  using Gauss's forward interpolation formula.
- (2) If  $f(x) = x^{-1}$  then find  $f(2, 5, 9, 10)$ .

(C) Answer any one : 3

- (1) Prove that divided differences are symmetric in all their arguments.
- (2) If  $f(x) = x^{-1}$  then show that  $f(x_0, x_1, \dots, x_n) = \frac{(-1)^n}{x_0 x_1 \dots x_n}$

(D) Answer any one : 5

- (1) Taking  $x = a, b, c, d$  find first three divided differences of

$$\frac{1}{x^2}$$

- (2) Apply Lagrange's formula inversely to find the root of  $f(x) = 0$  given that  $f(30) = -30, f(34) = -13, f(35) = 3, f(42) = 18$ .

4 (A) Answer the following questions : 4

- (1)  $\frac{dy}{dx}$  at  $x=x_0$  = \_\_\_\_\_. Fill in the blank.
- (2) What is the general quadrature formula ?
- (3) Which value of n in general quadrature formula gives trapezoidal rule ?
- (4) Write Simpson's  $\frac{3}{8}$  rule.

(B) Answer any one : 2

(1) In usual notation prove that

$$D = \frac{1}{h} \left( \nabla + \frac{\nabla^2}{2} + \frac{\nabla^3}{3} + \frac{\nabla^4}{4} + \dots \right)$$

(2) Find the value of  $\int_2^6 \frac{dx}{x}$  by trapezoidal rule.

(C) Answer any one : 3

(1) Derive general quadrature formula.

(2) In usual notation prove that  $D^3 = \left[ \nabla^3 + \frac{3}{2} \nabla^4 + \frac{7}{4} \nabla^5 + \dots \right]$

(D) Answer any one of following : 5

(1) Derive formula of derivatives using Newton's forward formula.

(2) Find Second derivative of  $f(x)$  at 1.5 for the following table.

$X$	1.5	2	2.5	3	3.5	4
$F(x)$	3.375	7	13.625	24	38.875	59

5 (A) Answer the following questions : 4

(1) In Milne's predictor formula, integration is taken in the interval \_\_\_\_\_. Fill in the blank.

(2) Find the value of  $k_1$  in the solution of

$$\frac{dy}{dx} = 3x + y^2, y(1) = 1.2 \text{ by Range's method.}$$

(3) Find the value of  $y$  at  $x = 0.2$  by Euler's method :

$$\frac{dy}{dx} = 2x + y, y(0) = 1$$

(4) Write Milne's Corrector formula.

(B) Answer any one : 2

(1) Explain Taylor's method to solve ordinary differential equation.

(2) Use Euler's modified method to obtain  $y(0.25)$  given that  $y' = 2xy, y(0) = 1$

(C) Answer any one : 3

(1) Explain Picard's method to solve ordinary differential equation.

(2) Explain Euler's improved method.

(D) Answer any one : 5

(1) Explain Range's method.

(2) Explain Range's Kutta's method.